

# Introduction to Error Control Coding and Channel Coding Theorem

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# Outline

## 1 Introduction

## 2 Problem Statement

## 3 Framework of Communication System

## 4 Shannon Limit

## 5 Historical Milestones

## 6 Outline of the Course

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- Digital communication part of live.
- Shannon's landmark paper (1948).
- An era of error control coding.
- Close-to-bound error correcting codes.
- Turbo codes, low-density parity-check codes.



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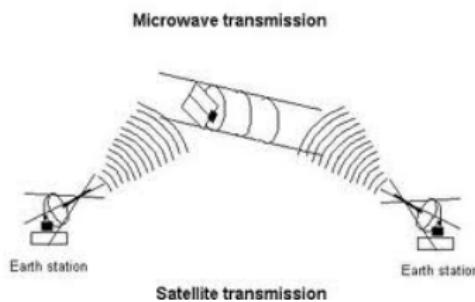
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- What is the aim?



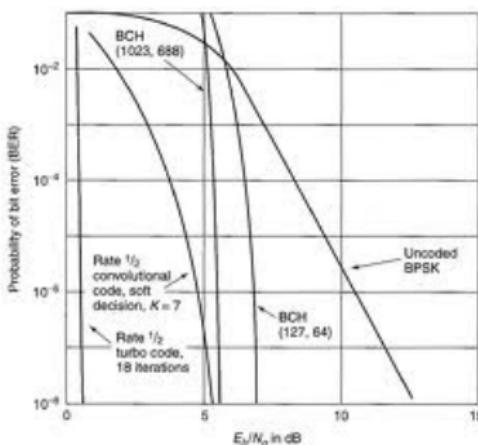
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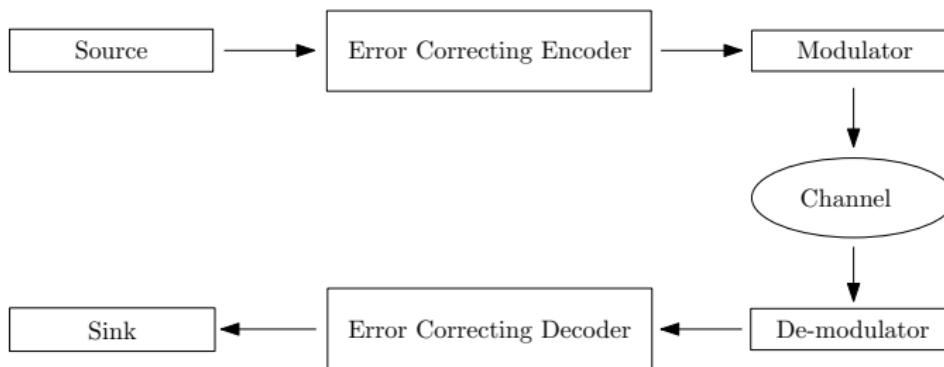


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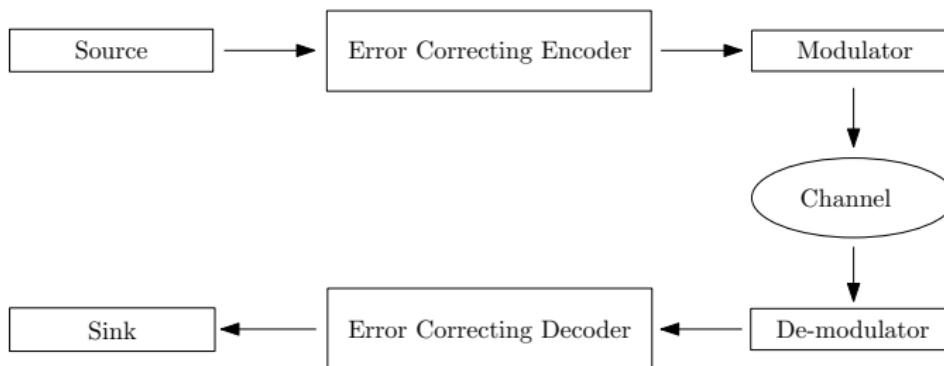
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- Source coding and modulation coding.
- Image, computer data, voice etc.
- ARQ/FEC



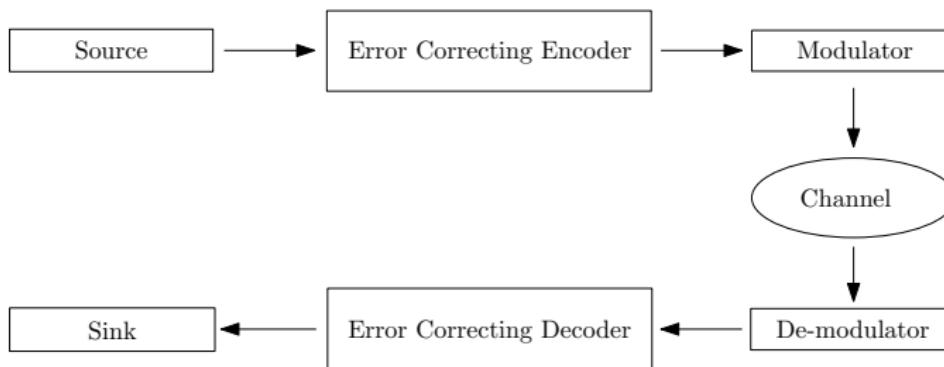
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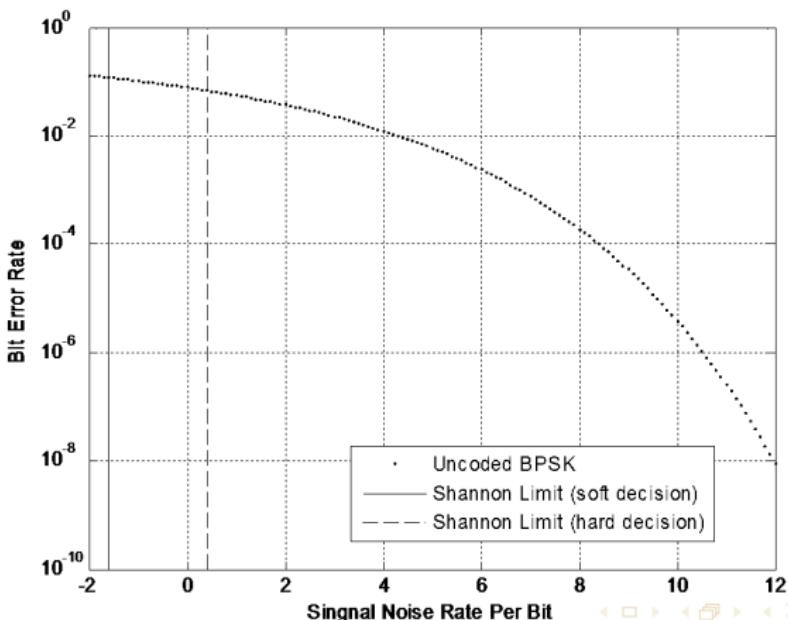


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# Shannon Limit

$$C = B \log_2\left(1 + \frac{S}{N}\right) \text{ bits/sec,}$$



# Milestones

- Channel Coding Theorem (1948).
- Hamming Codes (1950).
- Convolutional Codes (1955).
- Cyclic Codes (1957)
- BCH, Reed-Solomon Codes and Decoding Algorithm (1960)
- LDPC Codes (1962)
- 2400 bps modem commercially available
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