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University of the Witwatersrand, Johannesburg

Course or topic No(s) $\square$

Course or topic name(s)
Paper Number \& title

Examination/Test* to be
held during month(s) of
(*delete as applicable)
Year of Study
(Art \& Sciences leave blank)

Degrees/Diplomas for which
this course is prescribed
(BSc (Eng) should indicate which branch)

Faculty/ies presenting candidates

Data and Information Management
$\square$
$\square$
B.Sc (Eng) Elec.
$\square$

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| Course <br> Nos | ELEN3015 | Hours | Three |
| :---: | :---: | :---: | :---: |

Instructions to candidates (Examiners may wish to use this space to indicate, inter alia, the contribution made by this examination or test towards the year mark, if appropriate)

Answer ALL questions.
Type '2' Examination.

Internal Examiners or Heads of Department are requested to sign the declaration overleaf

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Note: Show all workings, complete with the necessary comments. Marks will be allocated for all working and logical reasoning and not just for the correct answer.

## Question 1

Describe a combined strategy making use of the method of Kasiski and the Incidence of Coincidence to decipher polyalphabetic enciphered text where the number of alphabets are known to be less than 5 .
( Total 5 marks)

## Question 2

The following questions refer to the DES algorithm.
(a) When is a key a weak key, a semi-weak key, or a possibly weak key?
( 3 marks)
(b) The following data stream is used as input to the S-Box Substitution of a specific round (In little-endian Format):

$$
A E A A 77 B 8 C 850
$$

Determine the output of the S-Box Substitution.

## Question 3

(a) What are the two most important properties of a secure hash function?
( 2 marks)
(b) With reference to hash algorithms, explain what the birthday attack is and how the threat of this attack affects the choice of a hash algorithm's hash size. (Note: probability calculations are not required).
( 6 marks)

## Question 4

(a) Write a small pseudocode algorithm for determining the value of $a^{b} \bmod p$. Assume that $a$ is smaller than $p$. Further assume that the underlying architecture can handle numbers smaller or equal to $p^{2}$. (You can make use of the function $a \bmod p$ )
(b) One of the steps in the Solovay-Strassen primality test is to compute the GCD of the candidate prime $p$ and a witness $a$. Calculate the GCD of the following numbers and comment on the outcomes and how the outcomes effect the primality testing:

- $\mathrm{p}=16100023, \mathrm{a}=121003$
- $\mathrm{p}=700781, \mathrm{a}=5003$
(c) Determine the Jacobi symbol J(1235/20003).
(d) Encrypt the message 00054 using RSA encryption. For the particular encryption, assume $p=109, q=107$ and the decryption key $d=8501$.
Hint 1:

$$
\begin{aligned}
8501 \times e_{1} & =73 \times Q+r_{1} \\
8501 \times e_{2} & =74 \times Q+r_{2} \\
8501 \times e_{3} & =75 \times Q+r_{3}
\end{aligned}
$$

Hint 2: $54^{99} \equiv 11042$, using the specified modular arithmetic.

## Question 5

Determine all the codewords of the $(n, k)$ linear code $C$ with parity-check matrix

$$
H=\left[\begin{array}{lllllll}
1 & 1 & 0 & 1 & 0 & 0 & 1 \\
0 & 0 & 0 & 1 & 1 & 0 & 1 \\
1 & 0 & 1 & 1 & 0 & 0 & 1 \\
0 & 0 & 0 & 0 & 0 & 1 & 1
\end{array}\right]
$$

Determine the parameters $n, k$ and $d_{\text {min }}$ of this code.

## Question 6

Do a systematic encoding of the following binary data using a Reed-Solomon code with $n$ $=7$ :

$$
011101110111001 .
$$

State the parameters $\left(n, k, d_{\text {min }}\right.$ and $\left.t\right)$ of the code and show all intermediate steps. Hint: Table 1 lists some primitive polynomials.

Table 1: Primitive polynomials

$$
\begin{gathered}
1+x+x^{3} \\
1+x+x^{4} \\
1+x^{2}+x^{5} \\
1+x+x^{6}
\end{gathered}
$$

## Question 7

Consider the following string of data:

## BDBGFBAGBDFGFABGGBGABFAABADBAA.

(a) Determine the entropy of the source based on the sample string.
(b) Encode the text using a Huffman code.

## Question 8

Discuss the JPEG still image compression standard. (Hint: Sketch the block diagram and discuss why each step in the compression process is needed and how each step is performed.)

## Question 9

(a) Suppose the student mark system data contains records like this.

| ID number | Student Number | Course | Mark |
| :--- | :--- | :--- | :--- |
| 861234123 | 06123456 a | ELEN0001 | 80 |
| 861234123 | 06123456 a | ELEN0003 | 70 |
| 861234123 | 06123456 a | ELEN0004 | 60 |
| 867761123 | 06244191 b | ELEN0001 | 53 |
| 867761123 | 06244191 b | ELEN0002 | 66 |
| 867761123 | 06244191 b | ELEN0004 | 58 |
| 867761123 | 06244191 b | ELEN0003 | 91 |
| 865331726 | 06009345 h | HART0001 | 72 |
| 865331726 | 06009345 h | ENGL0001 | 78 |
| 865331726 | 06009345 h | FREB0001 | 52 |

(i) State one problem with recording data like this.
(ii) Normalise the data to at least second normal form.
(b) A SNP is a position in a genetic sequence where some individuals in a population might have one character appearing and other individuals have another character (we always assume there are exactly two options). For example, I might have the character C appearing at a SNP and you might have a G. A SNP's location is given by the chromosome in which it appears and a location as measured from the beginning of the sequence.
The SNP table consists of a SNP identifier (text), the chromosome on which the SNP appears (a one or two letter code), its position (an integer), and a description of what the two alternatives for the SNP, which drawn from the set A, C, G, T, and -. There are 25 possible SNP alternatives: A/C, A/G, A/T, A/-, C/C, C/G, ...
The table below is an example. The first row says than SNP rs 15001218 appears in chromosome Z at position 22660621 and the two possible characters that can appear are G and T (these are always given in alphabetic order).

```
rs15001218,Z,22660621,G/T
rs15712282,10,22661114,C/T
rs15712280,10,22661127,A/G
rs13788418,10,22661285,C/G
```

In an experiment, we sample individuals from a population and record for each individual which SNPs were tested and what character was found. Our experiment table is shown below. The columns are the ID number of the individual sampled, the SNP tested, and which letter was found in the individual. For example, in the table A0001 was tested and two SNPs were found - in rs15001201, she had the symbol G, in rs15001202 she had the symbol C.

```
A0001,rs15001202,C
A0001,rs15001201,G
A0002,rs15712285,C
A0002,rs15001219,G
```


## Give good SQL code that can be used for the following

(i) Give the SQL to create a table called exps which can store the necessary information for the experiments conducted (i.e. which experimental subjects had which SNP).
( 2 marks)
(ii) Give the SQL that would find which SNPs were tested on experimental subject A1234.
( 1 marks)
(iii) Give the SQL that would list the IDs for all the experimental candidates which were tested for an SNP on chromosome $Z$.
( 2 marks)
(iv) Give the SQL that would find list the IDs for all the experimental candidates which were tested for an SNP on chromosome $Z$ where one of the alternative symbols for the SNP is a $C$. You need only write what addition you would make to the previous query.
(c) (i) Why are suffix arrays a useful technique for text databases?
(ii) Give the suffix array for orangesandlemonssay.

## Appendix A

Table 2: Key Permutation

| 57 | 49 | 41 | 33 | 25 | 17 | 9 | 1 | 58 | 50 | 42 | 34 | 26 | 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 2 | 59 | 51 | 43 | 35 | 27 | 19 | 11 | 3 | 60 | 52 | 44 | 36 |
| 63 | 55 | 47 | 39 | 31 | 23 | 15 | 7 | 62 | 54 | 46 | 38 | 30 | 22 |
| 14 | 6 | 61 | 53 | 45 | 37 | 29 | 21 | 13 | 5 | 28 | 20 | 12 | 4 |

Table 3: Number of Key Bits Shifted per Round

| Round | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Shifts | 1 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |

Table 4: Compression Permutation

| 14 | 17 | 11 | 24 | 1 | 5 | 3 | 28 | 15 | 6 | 21 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 23 | 19 | 12 | 4 | 26 | 8 | 16 | 7 | 27 | 20 | 13 | 2 |
| 41 | 52 | 31 | 37 | 47 | 55 | 30 | 40 | 51 | 45 | 33 | 48 |
| 44 | 49 | 39 | 56 | 34 | 53 | 46 | 42 | 50 | 36 | 29 | 32 |

Table 5: S-Box 1

| 14 | 4 | 13 | 1 | 2 | 15 | 11 | 8 | 3 | 10 | 6 | 12 | 5 | 9 | 0 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 15 | 7 | 4 | 14 | 2 | 13 | 1 | 10 | 6 | 12 | 11 | 9 | 5 | 3 | 8 |
| 4 | 1 | 14 | 8 | 13 | 6 | 2 | 11 | 15 | 12 | 9 | 7 | 3 | 10 | 5 | 0 |
| 15 | 12 | 8 | 2 | 4 | 9 | 1 | 7 | 5 | 11 | 3 | 14 | 10 | 0 | 6 | 13 |

Table 6: S-Box 2

| 15 | 1 | 8 | 14 | 6 | 11 | 3 | 4 | 9 | 7 | 2 | 13 | 12 | 0 | 5 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | 13 | 4 | 7 | 15 | 2 | 8 | 14 | 12 | 0 | 1 | 10 | 6 | 9 | 11 | 5 |
| 0 | 14 | 7 | 11 | 10 | 4 | 13 | 1 | 5 | 8 | 12 | 6 | 9 | 3 | 2 | 15 |
| 13 | 8 | 10 | 1 | 3 | 15 | 4 | 2 | 11 | 6 | 7 | 12 | 0 | 5 | 14 | 9 |

Table 7: S-Box 3

| 10 | 0 | 9 | 14 | 6 | 3 | 15 | 5 | 1 | 13 | 12 | 7 | 11 | 4 | 2 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | 7 | 0 | 9 | 3 | 4 | 6 | 10 | 2 | 8 | 5 | 14 | 12 | 11 | 15 | 1 |
| 13 | 6 | 4 | 9 | 8 | 15 | 3 | 0 | 11 | 1 | 2 | 12 | 5 | 10 | 14 | 7 |
| 1 | 10 | 13 | 0 | 6 | 9 | 8 | 7 | 4 | 15 | 14 | 3 | 11 | 5 | 2 | 12 |

Table 8: S-Box 4

| 7 | 13 | 14 | 3 | 0 | 6 | 9 | 10 | 1 | 2 | 8 | 5 | 11 | 12 | 4 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | 8 | 11 | 5 | 6 | 15 | 0 | 3 | 4 | 7 | 2 | 12 | 1 | 10 | 14 | 9 |
| 10 | 6 | 9 | 0 | 12 | 11 | 7 | 13 | 15 | 1 | 3 | 14 | 5 | 2 | 8 | 4 |
| 3 | 15 | 0 | 6 | 10 | 1 | 13 | 8 | 9 | 4 | 5 | 11 | 12 | 7 | 2 | 14 |

Table 9: S-Box 5

| 2 | 12 | 4 | 1 | 7 | 10 | 11 | 6 | 8 | 5 | 3 | 15 | 13 | 0 | 14 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14 | 11 | 2 | 12 | 4 | 7 | 13 | 1 | 5 | 0 | 15 | 10 | 3 | 9 | 8 | 6 |
| 4 | 2 | 1 | 11 | 10 | 13 | 7 | 8 | 15 | 9 | 12 | 5 | 6 | 3 | 0 | 14 |
| 11 | 8 | 12 | 7 | 1 | 14 | 2 | 13 | 6 | 15 | 0 | 9 | 10 | 4 | 5 | 3 |

Table 10: S-Box 6

| 12 | 1 | 10 | 15 | 9 | 2 | 6 | 8 | 0 | 13 | 3 | 4 | 14 | 7 | 5 | 11 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | 15 | 4 | 2 | 7 | 12 | 9 | 5 | 6 | 1 | 13 | 14 | 0 | 11 | 3 | 8 |
| 9 | 14 | 15 | 5 | 2 | 8 | 12 | 3 | 7 | 0 | 4 | 10 | 1 | 13 | 11 | 6 |
| 4 | 3 | 2 | 12 | 9 | 5 | 15 | 10 | 11 | 14 | 1 | 7 | 6 | 0 | 8 | 13 |

Table 11: S-Box 7

| 4 | 11 | 2 | 14 | 15 | 0 | 8 | 13 | 3 | 12 | 9 | 7 | 5 | 10 | 6 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 13 | 0 | 11 | 7 | 4 | 9 | 1 | 10 | 14 | 3 | 5 | 12 | 2 | 15 | 8 | 6 |
| 1 | 4 | 11 | 13 | 12 | 3 | 7 | 14 | 10 | 15 | 6 | 8 | 0 | 5 | 9 | 2 |
| 6 | 11 | 13 | 8 | 1 | 4 | 10 | 7 | 9 | 5 | 0 | 15 | 14 | 2 | 3 | 12 |

Table 12: S-Box 8

| 13 | 2 | 8 | 4 | 6 | 15 | 11 | 1 | 10 | 9 | 3 | 14 | 5 | 0 | 12 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 15 | 13 | 8 | 10 | 3 | 7 | 4 | 12 | 5 | 6 | 11 | 0 | 14 | 9 | 2 |
| 7 | 11 | 4 | 1 | 9 | 12 | 14 | 2 | 0 | 6 | 10 | 13 | 15 | 3 | 5 | 8 |
| 2 | 1 | 14 | 7 | 4 | 10 | 8 | 13 | 15 | 12 | 9 | 0 | 3 | 5 | 6 | 11 |

