## UNIVERSITY OF THE WITWATERSRAND, JOHANNESBURG

## SCHOOL OF ELECTRICAL AND INFORMATION ENGINEERING

## ELEN2008 Electric Circuits:

EXAMINATION June 2015

| Internal Examiner: | Prof Estelle Trengove |
| :--- | :--- |
| External Examiner: | Prof HE Hanrahan |

TOTAL MARKS: 100
TIME: 3 hours

## Instructions

Answer ALL questions. There are 110 possible marks, but the paper will be marked out of 100.

## Knowledge Area 1: Basic Concepts [40 marks]

## Question 1 [40 marks]

Note: Where indicated, solutions to this question must be entered on the sheet supplied. The final answer only is to be shown. Do not include any working on the sheet.


Figure 1: Six circuits containing various configurations of sources, resistors, capacitors and inductors
a) Enter the values on the sheet supplied for $v_{l}$ and $v_{2}$ for the circuit shown in Figure 1 (i). Indicate whether each source is supplying or absorbing power and how much power is being supplied/absorbed. Do not show any working on the sheet.
(6 marks)
b) For the circuit shown in Figure 1 (ii) enter the value for $v_{3}$ on the sheet supplied. Indicate whether each source is supplying or absorbing power and how much power is being supplied/absorbed. Do not show any working on the sheet.
c) For the circuit shown in Figure 1 (iii) calculate and enter the values for $i_{2}, i_{3}, i_{4}$ and $v_{5}$ on the sheet supplied. (Hint: to calculate $i_{2}$ you will have to reduce the circuit to a source and a single resistor.) Do not show any working on the sheet.
(7 marks)
d) On the answer sheet provided, calculate and enter the impedances of the inductor and calculate and enter the values of voltages $v_{6}$ and $v_{7}$ and current $i_{6}$ for the circuit shown in Figure 1 (iv).
e) For the circuit shown in Figure 1 (v) calculate and enter the values for $i_{2}$ and $v_{4}$ on the sheet supplied. Indicate whether each source is supplying or absorbing power and how much power is being supplied/absorbed. Do not show any working on the sheet. (7 marks)
f) Answer this question in your exam script and not on the sheet provided. For the circuit shown in Figure 1 (vi):

- Determine the impedance of the capacitor.
- Determine the current $i_{8}$ using vectors and a phasor diagram (no complex mathematics)
(5 marks)


## Knowledge Area 2: Analysis techniques [30 marks]

## Question 2 (15 marks)

i. Consider the circuit shown in Figure 2. Use mesh analysis to set up simultaneous equations and solve your equations to find values for the mesh currents.
(6 marks)
ii. Consider the circuit shown in Figure 2. Use superposition to find the voltage across terminals $a$ and $b, v_{a b}$.


Figure 2: Circuit containing resistors and sources

## Question 3 (15 marks)



Figure 3: Resistive circuit with a voltage and a current source
a) Consider the circuit shown in Figure 3. Use nodal analysis and solve for all the node voltages.
b) Consider the different circuit analysis techniques that you know (mesh and nodal analysis, superposition and Thévenin's and Norton's theorems, which one would you regards as most suitable for analyzing the circuit in Figure 3? Explain why you consider the technique that you chose as the most suitable one.

## Knowledge Area 3: Laboratory concepts and techniques [20 marks]

## Question 4 (10 marks)



Figure 4: Two sinusoidal signals
Referring to Figure 4, determine the following:
a) Measure the phase shift between the two signals and give it in degrees and in radians;
b) The peak to peak voltage of each of the signals;
c) The period of each of the signals signals;
d) The frequency of each of the signals.

## Question 5 (10 marks)

Table 1: Resistor values and voltage measurements

| Resistor $(\Omega)$ | Voltage (V) | Current (mA) |
| :--- | :--- | :--- |
| 200 | 2 |  |
| 375 | 3 |  |
| 500 | 3.5 |  |
| 3000 | 6 |  |

Four different load resistors were placed in turn across the output of a circuit and, in each case, the voltage across the resistor was measured, as shown in Table 1.
a) Redraw Table 1, calculate the current in the load resistor in mA and enter the values in your table.
b) Draw a graph of the variables in Table 1 and use the graph to estimate the Thévenin equivalent and the Norton equivalent circuit values of the circuit. Draw the Thévenin and Norton equivalent circuits labeled with these values.

## Knowledge Area 4: Complex real circuits [20 marks]

## Question 6

a) Analyse the circuit in Figure 5 and calculate $v_{\text {out }}$ and $i_{\text {out }}$.


Figure 5: Circuit containing 3 operational amplifiers and two voltage sources
b) Analyse the circuit in Figure 6 and calculate $v_{o l}, v_{o 2}$ and $v_{o 3}$.
(10 marks)


Figure 6: Circuit containing three cascaded operational amplifiers

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## Examination June 2015: Answer sheet

Student number: $\qquad$ Row: $\qquad$ Seat: $\qquad$

Question 1(a) (6 marks)
$v_{l}=$ $\qquad$
$v_{2}=$ $\qquad$
Is the 2 mA source supplying or absorbing power? $\qquad$
How much power is the 2 mA source supplying or absorbing? $\qquad$ mW

Is the 9 V source supplying or absorbing power? $\qquad$
How much power is the 9 V source supplying or absorbing? $\qquad$ mW

Question 1(b) (7 marks)
$v_{3}=$ $\qquad$
Is the 8 mA source supplying or absorbing power? $\qquad$
How much power is the 8 mA source supplying or absorbing? $\qquad$ mW

Is the 11 V source supplying or absorbing power? $\qquad$
How much power is the 11 V source supplying or absorbing? $\qquad$ mW

Is the 7 V source supplying or absorbing power? $\qquad$
How much power is the 7 V source supplying or absorbing? $\qquad$ mW

Question 1(c) (7 marks)

Current $i_{2}$ in Figure 1 (iii) is $\qquad$

Current $i_{3}$ in Figure 1 (iii) is $\qquad$

Current $i_{4}$ in Figure 1 (iii) is $\qquad$

Voltage $v_{5}$ in Figure 1 (iii) is $\qquad$

Question 1(d) (6 marks)
Impedance of the inductor in Figure 1 (iv) is: $\qquad$

Current $i_{6}$ in Figure 1 (iv) is $\qquad$

Voltage $v_{6}$ in Figure 1 (iv) is $\qquad$

Voltage $v_{7}$ in Figure 1 (iv) is $\qquad$

Question 1(e) (7 marks)
Current $i_{7}$ in Figure 1 (v) is $\qquad$

The voltage $v_{8}=$ $\qquad$
Is the 12 mA source supplying or absorbing power? $\qquad$
How much power is the 12 mA source supplying or absorbing? $\qquad$ W

Is the dependant current source supplying or absorbing power? $\qquad$
How much power is the dependant current source supplying or absorbing? $\qquad$ W

Question 1(f) (7 marks)
Answer in your exam script, not on the sheet.

